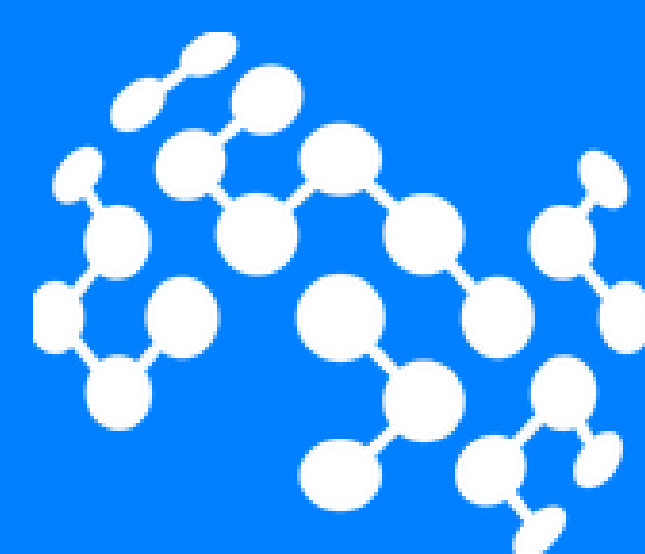


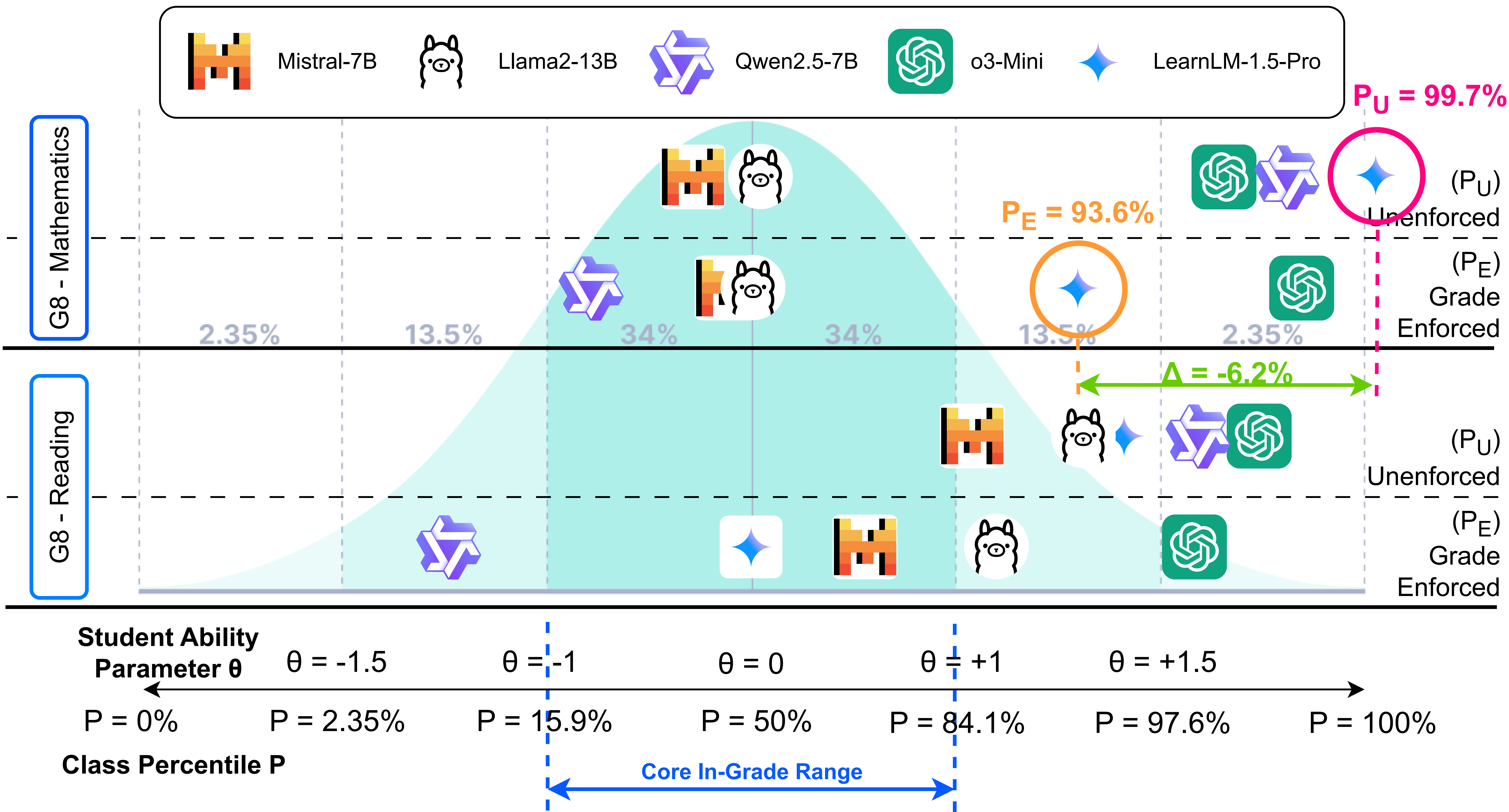


Can LLMs Reliably Simulate Real Students' Abilities in Mathematics and Reading Comprehension?

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Problem Statement

Can LLMs faithfully emulate the response patterns of students **of a specific grade**?

Motivation

Access to real student data is challenging.
Using LLM-based proxy students can aid in
+ Evaluating and developing tutoring systems
+ Pilot testing new assessments.

Method

We compare LLMs' performance on MCQ test questions from the **National Assessment of Educational Progress (NAEP)** [1] with students' overall response behavior across grades.

Using a simple **Rasch model** from Item Response Theory (IRT), we determine each model's ability parameter (θ). Mapped to class percentile, the ability estimate allows us to compare an LLM's performance with that of the **average student of a given grade**.

An LLM with ability close to that of the average student ($\theta = 0$ or $P = 50\%$) is deemed better aligned [2].

We conduct our study in two settings:
1. **Unenforced:** Using a regular problem-solving prompt to measure native ability.

2. **Grade Enforced:** Explicitly instructing the model to "act" like the average student of a given grade. We test three prompts with successively greater descriptiveness.

I - Unenforced (P_U)

Mathematics: Strong models overshoot the average (no alignment with any grade). Weaker models (e.g., Mistral-7B) show better alignment.

Reading: LLMs generally struggle with reading problems and thus, show better alignment with grade 12.

Best Practices

Grade Alignment: Must fall within normative grade bands -- Core (15.9% - 84.1%).

Developmental Ordering: For cross-grade proxies, ensure proper performance gradation, i.e., $P_4 \leq P_8 \leq P_{12}$

Prompt Stability: Grade enforced performance is volatile and case-based. Stick to unenforced querying unless necessary.

References

[1] National Center for Education Statistics. 2022. The nation's report card: 2022 naep reading and mathematics assessments. <https://nces.ed.gov/nationsreportcard/>.

[2] Susan E. Embretson and Steven P. Reise. 2000. Item Response Theory for Psychologists. Multivariate Applications Series. Lawrence Erlbaum Associates, Mahwah, NJ.



Data & Code



Presentation



arXiv Paper

II - Grade Enforced (P_E)

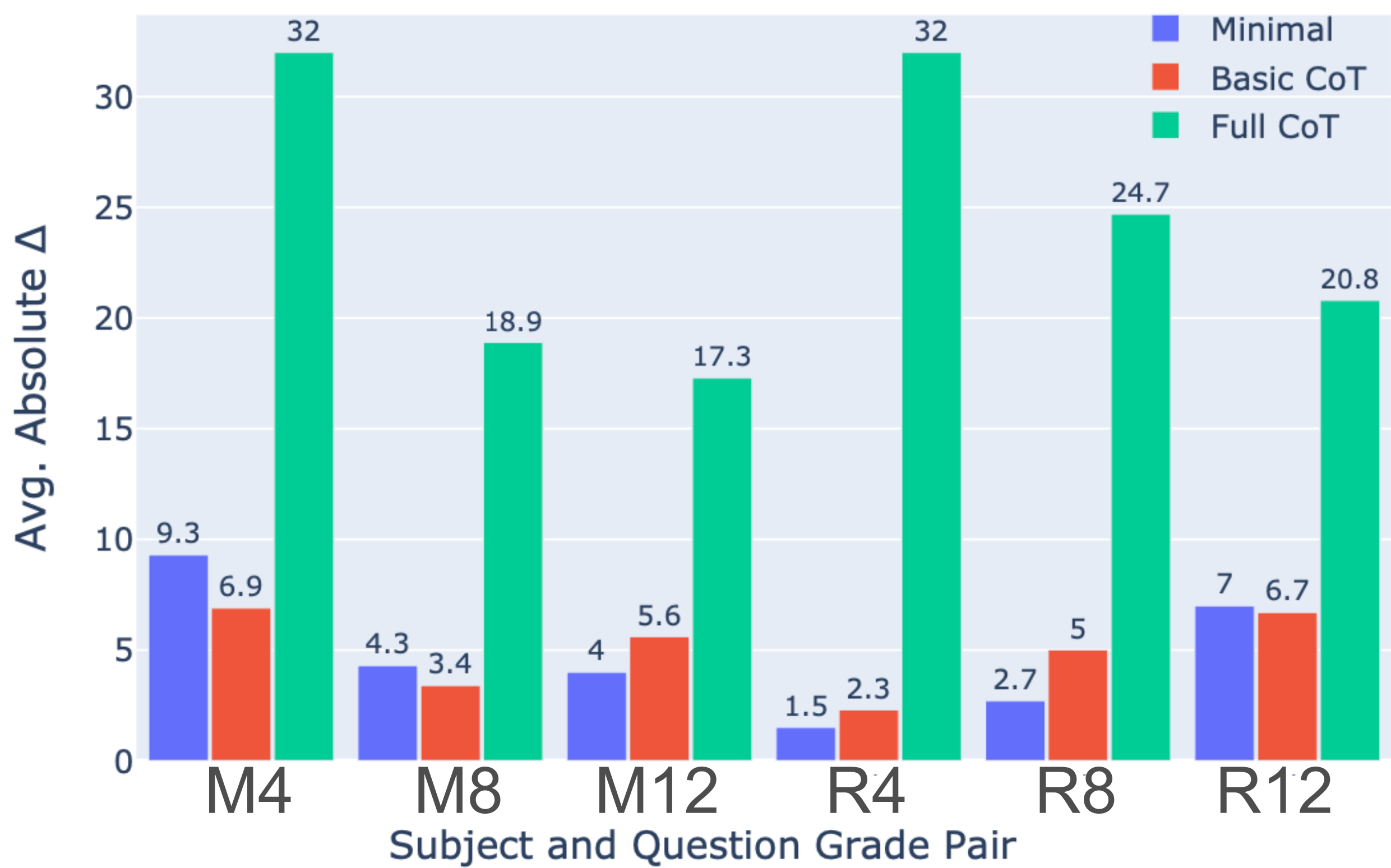
When testing grade enforcing prompts, we evaluate two aspects:

II - (a) Change ($\Delta = P_E - P_U$)

Drops: Greater drops for lower target grades.

Gains: LLM scores can improve when asked to mimic higher grade.

Prompt Strength: More descriptive prompting leads to greater shifts.



II - (b) Alignment

Alignment is possible; But, **no single prompt or model combination works always**.

Prompt Strength $\neq$ Accuracy: greater shifts do not always furnish better alignment.

No significant benefit from fine-tuning. Models tuned on math or pedagogical data do not exhibit better alignment than others.